

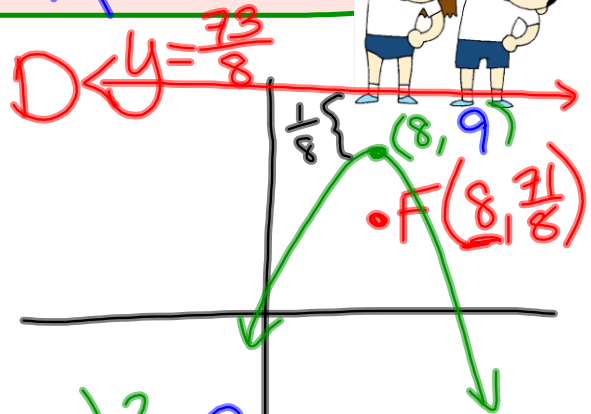
Warm Up: Given directrix $y = \frac{73}{8}$, and focus $(8, \frac{71}{8})$, write the equation of the quadratic in BOTH vertex and standard form.

$$y = \frac{1}{4p}(x-h)^2 + k$$

$\frac{73}{8}$
 Ans + 8.875
 Ans / 2

9.125
 18
 9

p = dist from
 • vertex to focus
 • vertex to directrix
 (h, k) = vertex



$$y = \frac{-1}{4(\frac{1}{8})}(x-8)^2 + 9$$

$$y = -2(x-8)^2 + 9$$

$$\frac{-1}{4(1/8)}$$

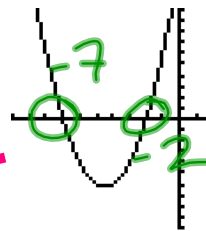
-2

Long Division of Polynomials

...remember long division from elementary school?

$$\begin{array}{r}
 \times 25 \text{ R } 3 \\
 5 \overline{) 128} \\
 \underline{-10} \downarrow \\
 28 \\
 \underline{-25} \\
 3
 \end{array}
 \qquad
 25 \frac{3}{5}$$

$$(x^2 + 9x + 14) / (x + 7)$$



how about factoring with dividing polynomials?

$$\frac{(x^2 + 9x + 14)}{(x + 7)} = \frac{(x+2)(\cancel{x+7})}{\cancel{x+7}} = \boxed{x+2}$$

But, what if you can't factor it and cancel common factors???

Example:

$$(3x^3 - 5x^2 + 10x - 3) / (3x + 1)$$

$$\begin{array}{r}
 x^2 - 2x + 4 \quad R - 7 \\
 3x + 1 \overline{) 3x^3 - 5x^2 + 10x - 3} \\
 \underline{- 3x^3 + 1x^2} \\
 -6x^2 + 10x \\
 \underline{- (+6x^2 + 2x)} \\
 12x - 3 \\
 \underline{- 12x + 4} \\
 -7
 \end{array}$$

$x^2 - 2x + 4 - \frac{7}{3x+1} \quad -7$

$3x+1$ isn't a factor, there's a remainder

Procedure:

- ① Rewrite as long division (LD) (*denom. outside of box)
- ② Find what you have to multiply the first term outside by to get the first term inside (distribute that to each term outside)
- ③ Subtract Result & bring down next term
- ④ Repeat 2-3 until there's no more terms

Regents Question 6/2016:

The expression $\frac{4x^3 + 5x + 10}{2x + 3}$ is equivalent to:

1) $2x^2 + 3x - 7 + \frac{31}{2x + 3}$

2) $2x^2 - 3x + 7 - \frac{11}{2x + 3}$

3) $2x^2 + 2.5x + 5 + \frac{15}{2x + 3}$

4) $2x^2 - 2.5x - 5 - \frac{20}{2x + 3}$



$$\begin{array}{r}
 \boxed{2x^2 - 3x + 7 - \frac{11}{2x+3}} \\
 \hline
 2x+3 \overline{) 4x^3 + 0x^2 + 5x + 10} \\
 \underline{-4x^3 + 6x^2} \\
 6x^2 + 5x \\
 \underline{+6x^2 + 9x} \\
 14x + 10 \\
 \underline{-14x + 21} \\
 -11
 \end{array}$$

Name: _____

SoftSchools

Polynomial Long Division.

1) $(6a^2 + 7a - 10) \div (a + 1)$

3) $(7a^2 - 20a + 24) \div (a - 3)$

5) $(6z^2 - 8z + 10) \div (z - 2)$

7) $(10c^2 + 12c - 15) \div (c + 3)$

9) $(9n^2 + 11n - 16) \div (n + 9)$

11) $(7m^4 + 16m^3 - 19m - 46) \div (m + 5)$

13) $(4c^4 + 10c^3 - 14c - 32) \div (c + 11)$

15) $(10a^4 + 19a^3 - 22a - 49) \div (a + 9)$

17) $(7c^4 - 4c^3 + 11c^2 - 8c - 8) \div (c - 3)$

19) $(4q^4 - 4q^3 + 20q^2 - 5q) \div (q - 10)$

2) $(7m^2 + 10m - 15) \div (m + 8)$

4) $(8b^2 + 10b - 12) \div (b + 2)$

6) $(8c^2 - 14c + 31) \div (c - 2)$

8) $(5y^2 + 8y - 11) \div (y + 7)$

10) $(5n^3 - 20n^2 + 24n - 76) \div (n - 10)$

12) $(x^4 + 11x^3 - 16x - 40) \div (x + 2)$

14) $(7n^4 - 6n^3 + 13n^2 - 6n) \div (n - 6)$

16) $(12z^4 - 10z^3 + 18z^2 - 6z - 12) \div (z - 7)$

18) $(8n^4 - 3n^3 + 8n^2 - 3n - 6) \div (n - 9)$

20) $(11y^4 - 8y^3 + 16y^2 - 10y - 11) \div (y - 6)$